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REMARKS ON NONGAUSSIAN LINEAR PROCESSES WITH ADDITIVE  
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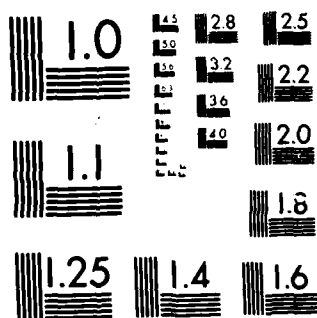
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REMARKS ON NONGAUSSIAN LINEAR PROCESSES  
WITH ADDITIVE GAUSSIAN NOISE\*

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The basic model. In a number of papers [1,2,4,5,6] nonGaussian linear processes are considered as the basic model. Questions relating to the estimation of coefficients and deconvolution were dealt with. We give the assumptions here. Let  $\{v_t\}$  be a sequence of independent, identically distributed random variables with  $E v_t = 0$ ,  $E v_t^2 = 1$  and some higher order cumulant  $\gamma_s \neq 0$  ( $s > 2$ ). The real coefficients  $\{\alpha_j\}$  are in  $\ell^2$

$$(1) \quad \sum \alpha_j^2 < \infty.$$

It's assumed that one observes the linear process

$$(2) \quad x_t = \sum_j \alpha_j v_{t-j}$$

without knowledge of the  $\alpha_j$ 's or the  $v_t$ 's. The object was to determine procedures for the estimation of the coefficients  $\alpha_j$  whether or not the system is minimum phase and effect deconvolution to estimate the  $v_t$ 's.

We shall still look at aspects of the problem just described. But our main concern will be with the modified problem in which we observe only

$$(3) \quad y_t = x_t + n_t$$

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where  $X_t$  has the structure given in (2) and  $\{n_t\}$  is a Gaussian noise process independent of the process  $\{X_t\}$ .

In many cases the spectral range of the  $X$  and  $n$  processes will be disjoint. In such a case direct linear filtering will let us get the process  $\{X_t\}$ . This happens, for example, when the spectrum of the  $n$ 's is in the high frequency range and that of the  $X$  process in the low frequency range. Suppose the interval  $[-a, a]$  contains the  $X$  spectral mass and that of the  $n$  process is outside. Further, let us assume that  $\pm a$  are continuity points of the spectral distribution function  $F$  of  $Y$ . The indicator function of  $[-a, a]$  has the Fourier representation

$$\sum_j \frac{1}{\pi} \frac{\sin ja}{j} e^{-ij\lambda}$$

and this implies that

$$X_t = \sum_j \frac{1}{\pi} \frac{\sin ja}{j} Y_{t-j}.$$

Dwyer [3] has been concerned with techniques aimed at gauging the Gaussian or nonGaussian character of additive components of the process  $Y$  corresponding to different spectral ranges. He tries to assess the third and fourth order moment properties of such components.

We shall be interested in seeing what happens when the spectral ranges of the  $X$  and  $n$  processes overlap. If the  $n$  process is small compared to the  $X$  process, one can still try to deconvolve approximately even by proceeding naively as if  $n$  weren't there. An example of such a naive convolution is given below. All this is independent of whether the system is minimum phase.

In Figures 1 and 2 the process  $Y_t$  is generated by a Monte Carlo simulation where

$$X_t = v_t - 3.5 v_{t-1} + 1.5 v_{t-2}$$

and  $v_t$  is a sequence of exponential independent random variables of variance one. Here the roots of the polynomial  $1 - 3.5z + 1.5z^2$  are 2 and  $1/3$ . The additive noise  $n_t$  consists of independent Gaussian variables of mean zero and variance  $\sigma^2 = 1$  in the case of Figure 1 and  $\sigma^2 = 2$  for Figure 2. The first line of the figure graphs the sequence

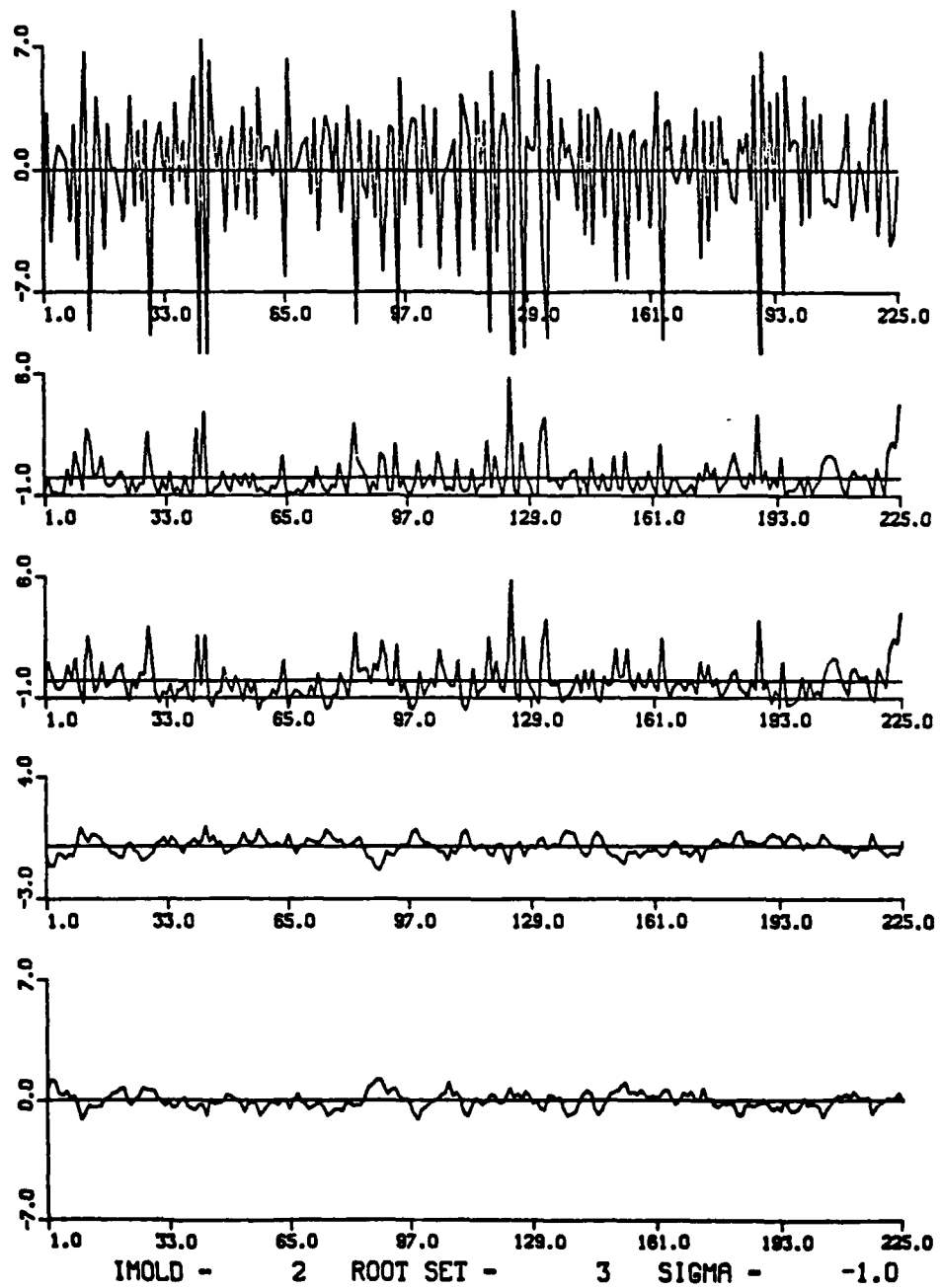


Figure 1.



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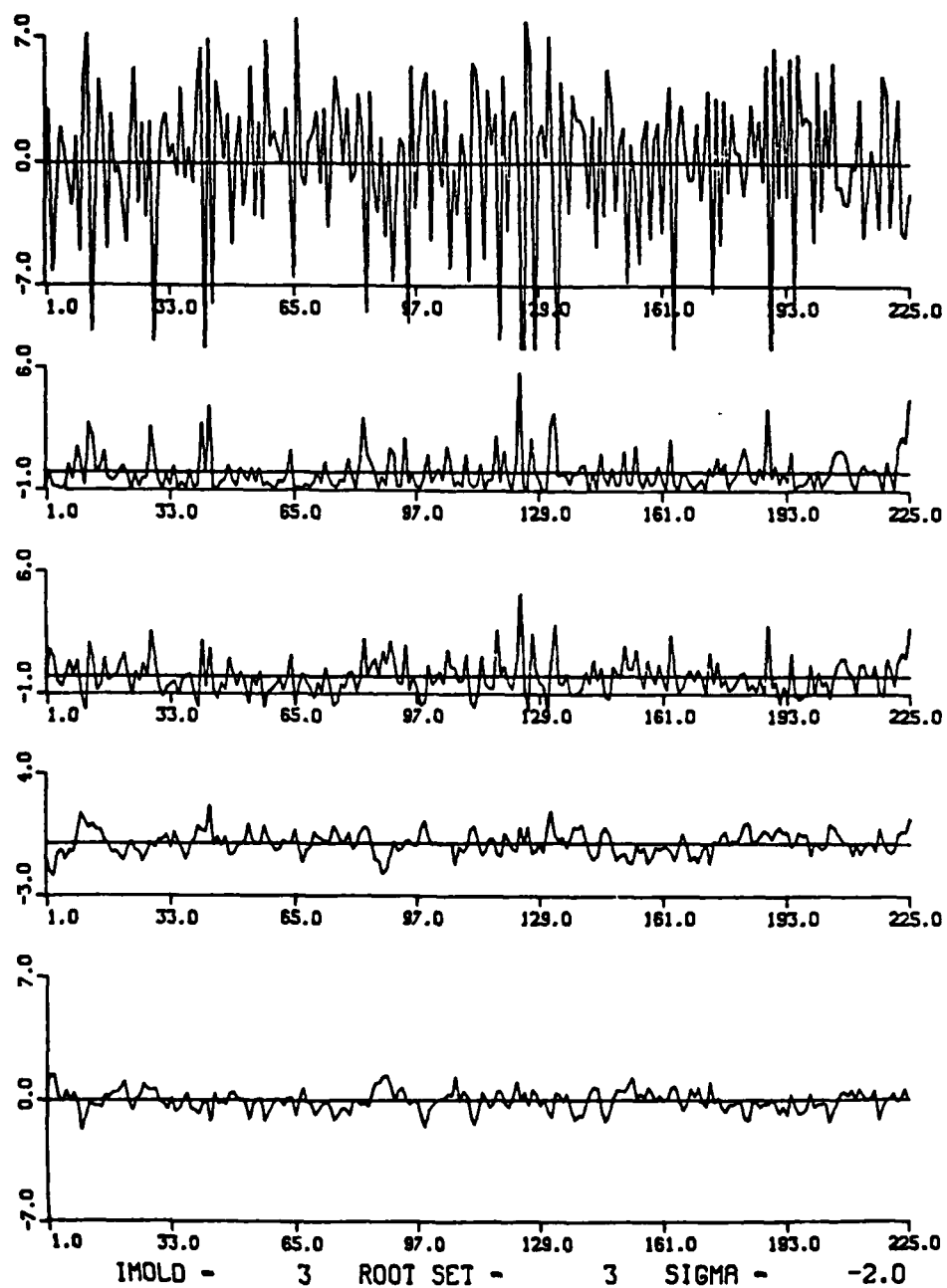


Figure 2.

$y_t$ . The second line graphs the generating  $v_t$  sequence. The third line gives the result of our naive deconvolution neglecting  $\eta$ . The fourth line gives the error in our deconvolution. The last line has the result of a minimum phase deconvolution which is naturally off because one of the roots is inside the unit disc in the complex plane. Clearly our naive deconvolution gets worse as  $\sigma^2$  increases. But even for  $\sigma^2 = 2$ , a moderate amount of noise, one can still recognize certain broad features of the  $v$  sequence. If  $\eta$  is large one won't be able to deconvolve but one can still hope to estimate a good deal about the  $\alpha_j$ 's under appropriate conditions.

A simple model. To give some idea of the difficulties that can arise, let us consider the case in which

$$(4) \quad y_t = a v_t + b u_t$$

with the  $\{v_t\}$  sequence nonGaussian independent, identically distributed with

$$E v_t \equiv 0, \quad E v_t^2 \equiv 1, \quad E v_t^3 \equiv \gamma \neq 0$$

and  $\{u_t\}$  an independent, identically distributed sequence of  $N(0,1)$  random variables. The  $\{v_t\}$  and  $\{u_t\}$  sequences are assumed to be independent. It is assumed that  $|a|$ ,  $|b|$  and  $\gamma$  are unknown. The counterpart of the problem mentioned above is that of estimating  $|a|$  and  $|b|$ .  $|a|$  and  $|b|$  are not identifiable in terms of the problem as specified here since  $v_t$  might be decomposable

$$(5) \quad v_t = v_t^{(1)} + v_t^{(2)}$$

in terms of two nontrivial independent summands, one of which, say  $v_t^{(2)}$ , is Gaussian. The problem can be normalized by insisting that  $v_t$  be indecomposable in the sense that a representation of the form (5) be impossible. We shall call a random variable  $v_t$  with a nontrivial decomposition of the form (5), in that a Gaussian summand with positive variance exists, reducible. This could be expressed in terms of distribution functions. A distribution will be called reducible if it has a nontrivial Gaussian component.

**PROPOSITION.** *A reducible distribution has a maximal decomposition relative to its Gaussian component.*

Let  $\varphi$  be the characteristic function of the reducible distribution. Then there are constants  $c_n > 0$  and corresponding characteristic functions  $\psi_n$  such that

$$\varphi(t) = \psi_n(t) \exp\left(-c_n \frac{t^2}{2}\right).$$

Then

$$\operatorname{Re} \varphi(t) \leq \operatorname{Re} \psi_n(t) \leq 1.$$

Let the  $F_n$  be the distributions corresponding to the characteristic functions  $\psi_n$ . We have

$$\begin{aligned} \int_{|x| \geq 1/u} dF_n(x) &\leq \frac{7}{u} \int_0^u \{1 - \operatorname{Re} \psi_n(v)\} dv \\ &\leq \frac{7}{u} \int_0^u \{1 - \operatorname{Re} \varphi(v)\} dv. \end{aligned}$$

We have then uniform bounds on the tails of the distributions  $F_n$ . One can therefore choose a subsequence  $F_{n_k}$  with  $c_{n_k} \uparrow c = \sup_n c$  that converges weakly. Let the limiting distribution be  $F$  with corresponding characteristic function  $\psi$ . It then follows that

$$(6) \quad \varphi(t) = \psi(t) \exp\left(-c \frac{t^2}{2}\right)$$

which corresponds to the unique maximal decomposition.

The problem of estimating  $|a|$ ,  $|b|$  now in (4) where  $v_t$  is irreducible is one in which  $|a|$ ,  $|b|$  are identifiable. However, the problem of deconvolution which is that of estimating  $v_t$  is clearly not meaningful.

The representation (6) implies that any distribution with a characteristic function  $\varphi(t)$  that doesn't decrease to zero as fast as the Gaussian as  $|t| \rightarrow \infty$  must be irreducible. This means that all discrete distributions and all gamma distributions must be irreducible.

Let's consider the question of predicting a  $v_t$  given  $y_t$ . We shall put this in the form

$$Y = \xi + \eta$$

where  $\xi$  and  $\eta$  are independent with means zero and variances  $\sigma_1^2$



and  $\sigma_2^2$  respectively.  $\eta$  is normal and  $\xi$  is nonnormal with density  $g(\cdot)$ . We are typically interested in the case in which  $\sigma_2^2$  is small compared to  $\sigma_1^2$ . The best linear predictor of  $\xi$  in mean square is  $\alpha Y$  where (assuming  $\sigma_1^2$  and  $\sigma_2^2$  known)

$$\alpha = \frac{\sigma_1^2}{\sigma_1^2 + \sigma_2^2}$$

and the variance of the prediction error is

$$\frac{\sigma_1^2 \sigma_2^2}{\sigma_1^2 + \sigma_2^2}.$$

The best predictor of  $\xi$  in mean square is  $E(\xi|Y)$ . Now

$$\begin{aligned} E(\xi^k|Y) &= \frac{\int \xi^k g(\xi) \frac{1}{\sqrt{2\pi\sigma_2^2}} \exp\left[-\frac{1}{2\sigma_2^2}(Y-\xi)^2\right] d\xi}{\int g(\xi) \frac{1}{\sqrt{2\pi\sigma_2^2}} \exp\left[-\frac{1}{2\sigma_2^2}(Y-\xi)^2\right] d\xi} \\ &= \frac{\frac{1}{\sqrt{2\pi}} \int (Y-u\sigma_2)^k g(Y-u\sigma_2) \exp\left(-\frac{1}{2}u^2\right) du}{\frac{1}{\sqrt{2\pi}} \int g(Y-u\sigma_2) \exp\left(-\frac{1}{2}u^2\right) du}. \end{aligned}$$

Let

$$m_k(Y) = \frac{\int u^k g(Y-u\sigma_2) \exp\left[-\frac{1}{2}u^2\right] du}{\int g(Y-u\sigma_2) \exp\left[-\frac{1}{2}u^2\right] du}.$$

Then

$$E(\xi^k|Y) = \sum_{j=0}^k \binom{k}{j} Y^{k-j} \sigma_2^j (-1)^j m_j(Y).$$

Assuming sufficient smoothness and using a Taylor expansion we have

$$g(Y-u\sigma_2) = g(Y) - u\sigma_2 g'(Y) + \frac{(u\sigma_2)^2}{2!} g''(Y) + \dots$$

and consequently the best predictor is

$$E(\xi|Y) = Y + \sigma_2^2 \frac{g''(Y) + \frac{\sigma_2^2}{2} g^{(3)}(Y) + \dots}{g(Y) + \frac{\sigma_2^2}{2} g''(Y) + \dots}$$

while

$$E(\xi^2|Y) = Y^2 + 2Y \sigma_2^2 \frac{g'(Y) + \frac{\sigma_2^2}{2} g^{(3)}(Y) + \dots}{g(Y) + \frac{\sigma_2^2}{2} g''(Y) + \dots} + \sigma_2^2 \frac{g(Y) + \frac{3}{2} \sigma_2^2 g''(Y) + \dots}{g(Y) + \frac{\sigma_2^2}{2} g''(Y) + \dots}.$$

We should like to compare,

$$E((\xi - \alpha Y)^2|Y) = E(\xi^2|Y) - 2\alpha Y E(\xi|Y) + \alpha^2 Y^2$$

with

$$E((\xi - E(\xi|Y))^2|Y) = E(\xi^2|Y) - E(\xi|Y)^2.$$

It is clear that

$$E((\xi - E(\xi|Y))^2|Y) \leq E((\xi - \alpha Y)^2|Y)$$

and the difference is given by

$$(\alpha Y - E(\xi|Y))^2 = ((1-\alpha)Y + \sigma_2^2 \frac{g'(Y)}{g(Y)} + o(\sigma_2^2))^2.$$

Such a comparison can give us some idea of the effectiveness of the best predictor versus the linear predictor in the tail region of the  $g$  distribution. This tail region may be of greatest interest in certain deconvolution problems (see Wiggins [6]).

Up to this point we have considered prediction in mean square. Suppose we consider instead trying to minimize

$$E|\xi - f(Y)|^4$$

for some appropriate  $f$  when  $Y = \xi + \eta$  with  $\eta \sim N(0, \sigma_2^2)$  and  $\xi$  irreducible nonnormal with mean zero and variance  $\sigma_1^2$ . An analysis can be carried out by considering

$$E(\xi - f(Y))^4 = E(E((\xi - f(Y))^4|Y)).$$

We can obviously minimize this if we can minimize the conditional fourth moment on the right side for each  $Y$ . This suggests that we consider minimizing

$$E(Z - c)^4$$

in  $c$  where  $Z$  is a random variable with  $E Z^4 < \infty$  and  $c$  is a constant. Let  $m$  be the mean of  $Z$  with  $\alpha = m - c$ . Then

$$(7) \quad E(Z - c)^4 = E(Z - m + \alpha)^4 = \alpha^4 + 6\sigma^2\alpha^2 + 4\mu_3\alpha + \mu_4$$

with  $\sigma^2$  the variance of  $Z$  and  $\mu_j$  the  $j^{\text{th}}$  central moment. Differentiating this with respect to  $\alpha$  we get

$$(8) \quad 4\alpha^3 + 12\sigma^2\alpha + 4\mu_3 = 0.$$

If  $\mu_3 = 0$  the unique real zero is  $\alpha = 0$  and the minimum is attained by  $c = m$ . If  $\mu_3 \neq 0$  we have a unique real zero since the derivative

$$12\alpha^2 + 12\sigma^2$$

of (8) is positive. The zero will be negative if  $\mu_3 > 0$  and positive if  $\mu_3 < 0$ . Set (8) equal to zero and solve for  $\alpha$ . By Cardano's formula one obtains

$$(9) \quad \alpha = 2^{-1/3} [-\mu_3 + \{\mu_3^2 + 4\sigma^6\}^{1/2}]^{1/3} - 2^{-1/3} [\mu_3 + \{\mu_3^2 + 4\sigma^6\}^{1/2}]^{1/3}.$$

This means that the function  $f(Y)$  minimizing (7) is

$$f(Y) = m(Y) - \alpha(Y)$$

where

$$m(Y) = E(\xi|Y)$$

and  $\alpha(Y)$  is given by expression (9) with

$$\mu_3 = E((\xi - E(\xi|Y))^3|Y)$$

and

$$\sigma^2 = E((\xi - E(\xi|Y))^2|Y).$$

Estimation of coefficients. Let  $\{Y_t\}$  be a process of type indicated in formula (3), that is, the sum of a linear non-Gaussian process and an independent Gaussian noise process. We shall indicate in a simple way that the coefficients  $\alpha_j$  of the linear nonGaussian process can be estimated up to an undetermined multiplier and an undetermined time shift. This is an asymptotic argument.

PROPOSITION. Let  $\{Y_t\}$  be a linear nonGaussian process perturbed by independent Gaussian noise. Suppose that  $\sum |k| |\alpha_k| < \infty$ ,  $\alpha(i^{-i\lambda}) \neq 0$  for all  $\lambda$  and  $\gamma_3 \neq 0$ . Then the coefficients  $\alpha_k$  can be consistently estimated up to an undetermined multiplier  $c$  and an unspecified time shift of the index set.

The bispectral density of the process  $\{Y_t\}$  is

$$b_3(\lambda_1, \lambda_2) = \frac{\gamma_3}{(2\pi)^2} \alpha(e^{-i\lambda_1}) \alpha(e^{-i\lambda_2}) \alpha(e^{i(\lambda_1 + \lambda_2)}) .$$

As before one can estimate the phase of  $\alpha(e^{-i\lambda})$  consistently up to an undetermined additive term  $ik\pi$  with  $k$  integral. This can be accomplished by using bispectral estimates as in Lii and Rosenblatt [4]. Notice that

$$(10) \quad b_3(\lambda, 0) = \frac{\gamma_3}{(2\pi)^2} \alpha(1) |\alpha(e^{-i\lambda})|^2 .$$

Bispectral estimates (using (10)) then allow us to estimate the spectral density of the process  $\{X_t\}$  up to an undetermined constant. The proposition follows immediately from these remarks.

Corollary. *Let the assumptions of the proposition be satisfied. Suppose that the Gaussian noise is white and that  $|\alpha(e^{-i\lambda})| \neq$  constant for all  $\lambda$ . One can then estimate the multiplier  $c$ . There is then only an unspecified time shift of the index set. The variance of  $n$  can also be estimated.*

Since the assumptions of the proposition are satisfied the conclusions hold. We have only to estimate the multiplier  $c$ . Both the spectral density

$$f_1(\lambda) = \frac{1}{2\pi} |\alpha(e^{-i\lambda})|^2 + \frac{\sigma_n^2}{2\pi}$$

of the  $Y$  process and

$$b(\lambda, 0) = \frac{\gamma_3}{(2\pi)^2} \alpha(1) |\alpha(e^{-i\lambda})|^2$$

can be estimated consistently. Clearly

$$\begin{aligned} f_1(\lambda) &= \frac{2\pi}{\gamma_3 \alpha(1)} b(\lambda, 0) + \frac{\sigma_n^2}{2\pi} \\ &= A b(\lambda, 0) + B . \end{aligned}$$

The coefficients  $A, B$  can be consistently estimated given consistent estimates of  $f_1(\lambda), b(\lambda, 0)$ . The conclusion then follows.

The argument of a polynomial transfer function. In many cases it seems reasonable to assume that  $\alpha(Z)$  is a polynomial

$$\alpha(Z) = \sum_{j=0}^p \alpha_j Z^j.$$

Because the coefficients are assumed real, the roots  $Z_j$  are real or occur in complex conjugate pairs. The argument of  $\alpha(e^{-i\lambda})$  is the sum of the contributions from the factors corresponding to the roots. We shall consider the contribution from a root  $Z_j$  with  $|Z_j| \neq 1$ . Suppose  $Z_j = re^{-i\theta}$  with  $0 < r < 1$  and  $-\pi < \theta \leq \pi$ . Then

$$\begin{aligned} \log(e^{-i\lambda} - Z_j) &= -i\lambda + \log(1 - e^{i\lambda} Z_j) \\ &= -i\lambda - \sum_{k=1}^{\infty} (e^{i\lambda} Z_j)^k / k \end{aligned}$$

and this implies that

$$(11) \quad \text{Im} \log(e^{-i\lambda} - Z_j) = -\lambda - \sum_{k=1}^{\infty} \frac{r^k \sin k(\lambda - \theta)}{k} \quad \text{for } |Z_j| < 1.$$

Similarly for  $Z_j = re^{-i\theta}$  with  $r > 1$  one has

$$\begin{aligned} \log(e^{-i\lambda} - Z_j) &= \log(-Z_j) + \log(1 - Z_j^{-1} e^{-i\lambda}) \\ &= i\pi + \log Z_j - \sum_{k=1}^{\infty} (Z_j^{-1} e^{-i\lambda})^k / k \end{aligned}$$

and this implies that we have a representation

$$(12) \quad \text{Im} \log(e^{-i\lambda} - Z_j) = \pi - \theta - \sum_{k=1}^{\infty} \frac{r^{-k} \sin k(\theta - \lambda)}{k}$$

for  $|Z_j| > 1$ . Let us formally consider the difference between (11) and (12) for  $r = 1$ , that is

$$(13) \quad \theta - \lambda - \pi + 2 \sum_{k=1}^{\infty} \frac{\sin k(\theta - \lambda)}{k}.$$

Notice that the Fourier series of  $x - \pi \operatorname{sgn} x$  is

$$-2 \sum_{k=1}^{\infty} \frac{2 \sin kx}{k}.$$

This implies that the expression (13) equals zero for  $0 < \theta - \lambda < \pi$  and  $-2\pi$  for  $-\pi < \theta - \lambda < 0$ . This is consistent with the indeterminacy of the argument up to a multiple of  $2\pi$ . For a real root  $|Z_j| < 1$  expression (11) becomes

$$- \lambda \pm \sum_{k=1}^{\infty} \frac{r^k \sin k\lambda}{k}$$

according as to whether  $\theta = 0$  or  $\pi$ . In the case of complex conjugate roots of absolute value less than one the sum of the contributions is

$$- 2\lambda - 2 \sum_{k=1}^{\infty} \frac{r^k \sin k\lambda \cos k\theta}{k}.$$

The corresponding remarks for roots greater than one read as follows. If  $|z_j| > 1$  is real expression (12) is

$$(1 - \delta_{\theta, \pi})\pi \pm \sum_{k=1}^{\infty} \frac{r^{-k} \sin k\lambda}{k}$$

with  $\pm$  according as to whether  $\theta = 0$  or  $\pi$ . If there are complex conjugate roots one obtains

$$2\pi + 2 \sum_{k=1}^{\infty} \frac{r^{-k} \sin k\lambda \cos k\theta}{k}.$$

In our case we try to estimate the sum of the contributions to the argument from all zeros and then as a convention re-adjust the value at zero of the sum so that it is zero there.

This discussion of the relationship between the argument of the transfer function and zeros of  $\alpha(Z)$  is natural when  $\alpha(Z)$  is a polynomial. A corresponding discussion could be carried out if  $\alpha(Z)$  is a rational function in terms of the zeros and poles of  $\alpha(Z)$ . However, one can easily give examples of analytic functions  $\alpha(Z)$  with no zeros such as, for example,

$$\alpha(Z) = \exp \{ \sin Z \}.$$

Here, there would be no meaning to such an analysis.

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